

$$g(z) = \frac{1}{z^2} + \sum_{(n,m) \in \mathbb{Z}^2 \setminus 0} \left(\frac{1}{z + 2m + 2in} \right)^2 - \left(\frac{1}{2m + 2in} \right)^2$$